



Practise Examination One MATHEMATICS: SPECIALIST

$\label{eq:Question/Answer Booklet - Section 1 - Calculators \, \underline{\it NOT} \ allowed - Notes \ sheets \, \underline{\it NOT} \ allowed$

Teacher's Name:

Time allowed for this paper

Section	Reading	Working
Calculator-free	5 minutes	50 minutes
Calculator-assumed	10 minutes	100 minutes

Materials required/recommended for this paper

Section One (Calculator-free): 50 marks

To be provided by the supervisor Section One Question/Answer booklet Formula sheet To be provided by the candidate Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters Special items: nil

Section Two (Calculator-assumed): 100 marks

To be provided by the supervisorSection Two Question/Answer bookletFormula sheet

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

Special items:drawing instruments, templates, notes on two unfolded sheets of A4 paper,
and up to three calculators satisfying the conditions set by the School
Curriculum and Standards Authority for this course.

Important Note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.



SEMESTER TWO EXAMINATION CALCULATOR-FREE

Instructions to candidates

- 1. All questions should be attempted.
- 2. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- 3. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you **do not use pencil** except in diagrams.

Structure of this paper

Questions	Marks available	Your score
1	11	
2	8	
3	10	
4	6	
5	8	
6	7	
Total:	50	
8	6	
9	11	
10	8	
11	7	
12	10	
13	8	
14	8	
15	11	
16	9	
17	4	
18	6	
19	7	
20	5	
Total:	100	
Total marks = 150		
		%

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SEMESTER TWO EXAMINATION SECTION ONE

Section One: Calculator-free

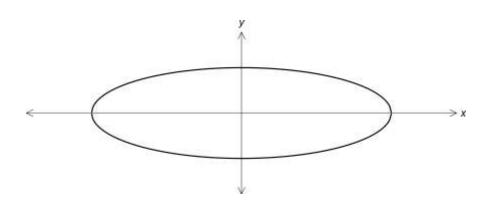
This section has six (6) questions. Answer all questions. Write your answers in the space provided.

Working time: 50 minutes.

Question 1

Consider the ellipse given by the following equation $\frac{x^2}{9} + \frac{y^2}{4} = 1$

(a) Find the volume of the solid of revolution that is generated by rotating about the *x*-axis and express your answer in terms of π .



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(11 marks)

(4)

(50 Marks)

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SEMESTER TWO EXAMINATION CALCULATOR-FREE

(b) Explain why the equation given by the ellipse is not a function. What restriction would you place on the equation to make it a function?

(2)

The path of a particle creates the ellipse and takes 12 seconds to complete a loop, starting at the position vector 3i metres moving in an anticlockwise direction.

(c) Find the vector equation of the position vector at any time, t, seconds.

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(d) Find the maximum velocity the particle reaches and the time it takes.

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SEMESTER TWO EXAMINATION SECTION ONE

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MATHEMATICS: SPECIALIST CALCULATOR FREE

Que	stion 2	(8 marks)
Two	complex numbers are given by $w = 2cis\frac{\pi}{3}$ and $z = \sqrt{3} - i$.	
(a)	Express in polar form	
	(i) <i>z</i>	(1)
	(ii) <i>w</i> ⋅ <i>z</i>	(1)
(b)	State the	
	(i) argument of $\frac{z}{w}$	(1)
	(ii) modulus of $\frac{1}{z}$	(1)

(c) Show that the product $w \cdot \overline{w}$ is purely real. (2)

(d) For what positive values of *n* is v_n purely real, given $v_{n+1} = v_n \times w$, $v_1 = w$?

(2)



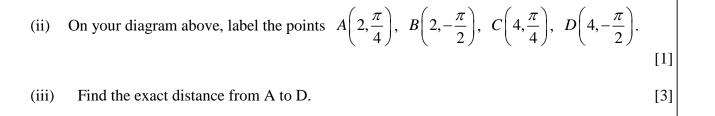
SEMESTER TWO EXAMINATION CALCULATOR-FREE

Question 3

(10 marks)

(a) (i) Sketch the region of the complex plane defined by:

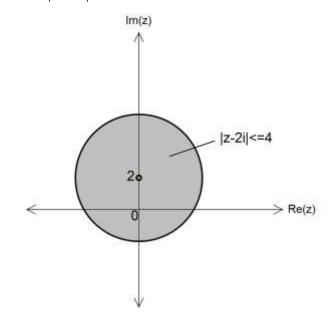
$$\left\{z: \frac{-\pi}{2} \le \arg z \le \frac{\pi}{4} \quad and \quad 2 \le |z| \le 4\right\}$$
[3]



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Question 3 continued

A locus of points defined by $|z-2i| \le 4$ is represented on the Argand diagram below.



(b) find the exact greatest and least values of |z-3+4i| in relation to the locus of points defined by $|z-2i| \le 4$.



[3]

SEMESTER TWO EXAMINATION CALCULATOR-FREE

(6 marks)

Evaluate
$$\int \frac{5x^2 + 1}{x^3 + x} dx$$

SEMESTER TWO EXAMINATION	
SECTION ONE	

Question 5

(8 marks)

(a) Integrate $\tan x \left(1 + \cos^2 x\right) dx$

[4]

[4]

(b) Solve $\frac{dy}{dx} = \frac{x+1}{y^4+1}$, given that when x = 2, y = 1.



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SEMESTER TWO EXAMINATION CALCULATOR-FREE

Question 6

(7 marks)

Two particles, A and B, are tracked in a laboratory experiment.

Particle A was observed to have initial position 2i - j + 8k cm and constant velocity vector -2i + 4j - 2k cm/s.

Particle B was observed to have initial position -2i + 3j - 9k cm and constant velocity vector 3i + 2j + 4k cm/s.

If the particles continue with these velocities, find the minimum distance between them in the subsequent motion and the time when this occurs.

Additional working space

Question number:





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SEMESTER TWO EXAMINATION CALCULATOR-FREE

Additional working space

Question number:

Additional working space

Question number:

MATHEMATICS: SPECIALIST 3C/3D CALCULATOR FREE



SEMESTER TWO EXAMINATION CALCULATOR-FREE

Additional working space

Question number:

Additional working space

Question number:

MATHEMATICS: SPECIALIST 3C/3D CALCULATOR FREE

